

### Note

## Microhardness, dilatometric and electrostriction studies on $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$ binary system

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Received 23 May 1997; accepted 8 October 1997

The author reports the microhardness, electrostrictive and thermal expansive coefficients of  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary system. Elastic stiffness coefficient of  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  has been calculated from the microhardness data; further the electrostrictive results of this binary are observed to be supportive to the microhardness data. Thermal expansion coefficient and crystallographic data of  $\text{NaH}_2\text{PO}_4$  and  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary are compared

$\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary system is reported earlier<sup>1</sup> to be tetragonal. In the present work, data on microhardness<sup>2-4</sup>, electrostriction<sup>5,6</sup> and dilatometry<sup>7</sup> were carried out. From microhardness data elastic constants<sup>8</sup> and yield stress<sup>9</sup> were obtained. Comparison has been made on microhardness and electrostrictive data on the reported<sup>10</sup>  $\text{NH}_4\text{H}_2\text{PO}_4$  and  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary. Results on the thermal expansion coefficient of  $\text{NaH}_2\text{PO}_4$  and its binary were discussed.

### Experimental Procedure

$\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  crystals were grown from aqueous solution. The weight fraction of  $\text{NaH}_2\text{PO}_4$  in the  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary is 90.62%, the method of growth is reported earlier<sup>1</sup>. Microhardness of  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  was determined using 160 mph microhardness tester fitted with Vickers diamond pyramid indenter and attached to a Carl-Zeiss [Jenavert] research microscope. For static indentation test, load  $p$  varying from 5 to 70 g were applied on the selected (100) face of the crystal over a fixed interval of time (10 s), and removed. The Vicker's hardness number (hereafter abbreviated as VHN)  $H_v$  was calculated using the relation  $H_v = 1.8544 (p/d^2) \text{ kg mm}^{-2}$  where  $p$  is the applied load in kg and  $d$  is the average diagonal length of the Vickers impression in mm after unloading. The elastic stiffness coefficient is

calculated using the relation<sup>8</sup>  $C_{ij} = H^{7/4}$ . Electrostriction and thermal expansion coefficients were determined using an optical interference technique<sup>11</sup> described elsewhere. Electrostriction coefficient is obtained using the relation<sup>12</sup>  $R_{ijkl} = A/l$  where  $A = (\lambda \times N \times C^2)/(2 \times V^2)$ .

### Results and Discussion

**Microhardness data**—Fig.1 illustrate the variation of hardness with indenter load and Fig.2 gives the variation of the logarithm of applied load ( $p$ ) with the logarithm of length of indentation ( $d$ ), which is called log-log plot of Meyer. Microhardness is found to decrease with increase of indenter load (5-10 g) and remains unaffected beyond 10 g. The microhardness number  $H_v$  turns out to be  $80 \pm 5 \text{ kg/mm}^2$  at 40 g load. Least square fit of the logarithm plot between length of indentation ( $d$ ) and load ( $p$ ) yielded a straight line (Fig.2). The slope of the this line gives the value of  $n$ , the work-hardening index. Onitsch<sup>13</sup> and Hanneman<sup>14</sup> have shown that the value of  $n$  comes out to be between 1 to 1.6 for hard materials and more than 1.6 for soft materials. The value of  $n$  for the  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  is found to be close to 2, hence it is classified as a soft material. From the Wooster's relation<sup>8</sup> ( $C_{ij} = H^{7/4}$ ) between elastic stiffness coefficient and hardness of a crystal, the value of  $C_{11}$  for the  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary is calculated to be  $12 \pm 1 \times 10^{11} \text{ CGS units}$ . The value of  $H_v$  for  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary ( $80 \pm 5 \text{ kg/mm}^2$ )

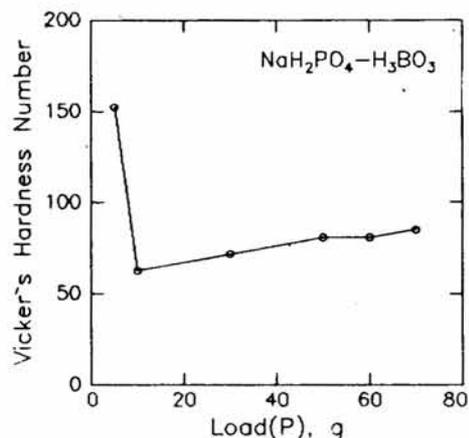


Fig.1—Variation of microhardness ( $H_v$ ) with load ( $p$ )

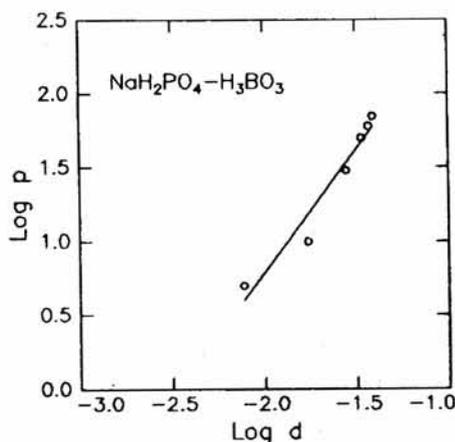


Fig. 2—Log-log plot of Meyer for  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary system

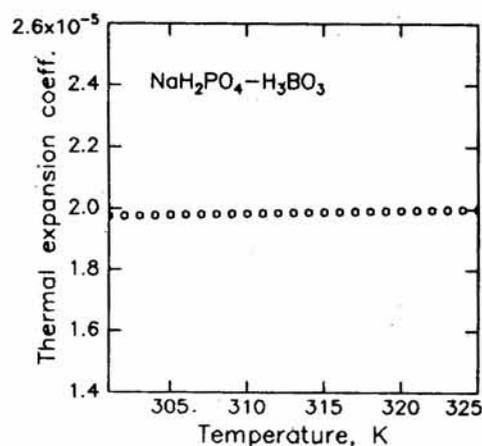


Fig. 3—Temperature variation of thermal expansion coefficient of the binary ( $\alpha_c$ )

is slightly higher compared to the reported<sup>10</sup> values of  $\text{NH}_4\text{H}_2\text{PO}_4$  ( $70 \pm 2 \text{ kg/mm}^2$ ) but lower than that of  $\text{KH}_2\text{PO}_4$  ( $160 \pm 2 \text{ kg/mm}^2$ ). This could be attributed to the difference in their molecular structure. The crystallographic structure of  $\text{NH}_4\text{H}_2\text{PO}_4$ ,  $\text{KH}_2\text{PO}_4$  and  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  are similar in  $\text{H}_2\text{PO}_4$  network and hence can be compared. In  $\text{NH}_4\text{H}_2\text{PO}_4$  the N-H...O bond occurs between ammonium and phosphate groups where as  $\text{KH}_2\text{PO}_4$  and  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  are polar structures consisting of  $\text{K}^+$  and  $\text{H}_2\text{PO}_4^-$  and  $\text{Na}^+$  and  $\text{H}_2\text{PO}_4^-$  ions respectively. The size of cations, the magnitude of electron affinity, electronegativity values of  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  are less in comparison with  $\text{NH}_4\text{H}_2\text{PO}_4$  but more with  $\text{KH}_2\text{PO}_4$ . In the light of these facts it is proposed that the ionic bonding between  $\text{Na}^+$  and  $\text{H}_2\text{PO}_4^-$  ions is weaker than the bonding between  $\text{K}^+$  and  $\text{H}_2\text{PO}_4^-$  ions but stronger than that of N-H...O bond occurring between ammonium and phosphate groups justifying the value of  $H_v$  for  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$ .

**Electrostriction data**—It is reported<sup>1</sup> that  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  belong to tetragonal system at ambient temperature with  $C_{4h}$  or  $C_4$  point group symmetry. These point groups evolve ten independent electrostrictive coefficients<sup>15</sup> which are given below

$$R_{1111} = R_{2222}, R_{1122} = R_{2211}, R_{1133} = R_{2233}, R_{1112} = -R_{2212}, R_{3311}, R_{3333}, R_{2323}, R_{2331} = -R_{3123}, R_{1211} = -R_{1222} \text{ and } R_{1212}$$

The measured electrostrictive coefficients are  $R_{1133} = R_{2233}$  and  $R_{1111} = R_{2222}$  and their values are

observed to be  $50 \times 10^{-18} \text{ m}^2/\text{V}^2$  and  $23 \times 10^{-18} \text{ m}^2/\text{V}^2$  respectively.

$\text{NH}_4\text{H}_2\text{PO}_4$  and  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  are reported<sup>16,17</sup> to belong to same crystallographic system. Hence the literature data<sup>10,11</sup> of microhardness and electrostrictive coefficient on  $\text{NH}_4\text{H}_2\text{PO}_4$  and  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  can be compared. It is known that higher value of VHN indicates stronger bonding of atoms in the sample, which in turn are expected to possess lower values of electrostrictive coefficients. It may be pointed out that the VHN value of  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  is greater than that of  $\text{NH}_4\text{H}_2\text{PO}_4$ . Thus the higher electrostrictive coefficient values of  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  in comparison to that of  $\text{NH}_4\text{H}_2\text{PO}_4$  is in concurrence with the microhardness studies.

**Dilatometry data**—Fig. 3 illustrates the thermal expansion coefficient measurement along c-axis ( $\alpha_c$ ) for a temperature range from 300 to 323 K and its value is found to vary from 19.75 to  $20 \times 10^{-6} \text{ K}^{-1}$ .  $\text{NaH}_2\text{PO}_4$  is reported<sup>17</sup> to be orthorhombic with lattice parameters  $a = 6.606 \text{ \AA}$ ,  $b = 7.275 \text{ \AA}$  and  $c = 11.384 \text{ \AA}$ . Thermal expansion coefficient of  $\text{NaH}_2\text{PO}_4$  is reported<sup>18</sup> to be 38, 33 and  $28.6 \times 10^{-6} \text{ K}^{-1}$  along  $a$ ,  $b$  and  $c$  axes respectively.  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  is reported<sup>1</sup> to be tetragonal, the weight fraction of  $\text{NaH}_2\text{PO}_4$  and  $\text{H}_3\text{BO}_3$  in the  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary are 90.62 and 9.38% respectively. Further, the lattice parameters of the  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  are  $a = 5.42 \text{ \AA}$  and  $c = 7.45 \text{ \AA}$ . The  $\alpha_c$  for the binary may be compared with its pure sample at room temperature. Since there is a decrement in the value of the corresponding lattice parameter ( $c$ -

axis) the same trend is reflected in the value of  $\alpha_c$  which is justified.

### Conclusions

1. The Vicker's hardness number ( $H_v$ ) of  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary is  $80 \pm 5$  kg/mm<sup>2</sup> at 40 g load.

2. The microhardness data of  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary is in concurrence with that of the electrostriction studies.

3. Thermal expansion coefficient ( $\alpha_c$ ) of  $\text{NaH}_2\text{PO}_4\text{-H}_3\text{BO}_3$  binary is in accordance with its structural data obtained from X-ray diffraction technique

### Acknowledgement

The author acknowledge the useful suggestions provided by Prof. V G K M Pisipati, Director, Centre for Liquid Crystal Research and Education, Nagarjuna University. Microhardness facility provided by S P Sengupta, Jadavpur is gratefully acknowledged.

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